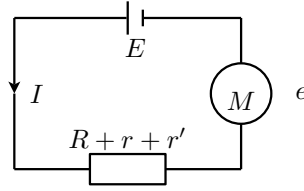


Exercice 1

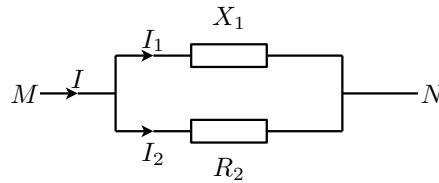
I) 1) Schéma équivalent :



Loi des mailles : $-E_1 + (R + r + r')I + e = 0$ (0,5),

$I = \frac{E_1 - e}{r + r' + R} = 1 \text{ A}$ (0,5)+(0,25), $V_M - V_N = RI = 30 \text{ V}$ (0,25).

2) $R_2 = X_2 + \frac{X_2}{2} = \frac{3}{2}X_2$ (0,5) (figure ci-dessous). $I_2 = I - I_1 = 0,25 \text{ A}$. (0,25)+(0,25)



$V_M - V_N = X_1 I_1$ (0,25), A.N. $X_1 = \frac{RI}{I_1} = 40 \Omega$ (0,25).

De même $V_M - V_N = \frac{3}{2}X_2 I_2$ (0,25), $X_2 = \frac{2RI}{3I_2} = 80 \Omega$ (0,25)

II) 1) Le courant est nul dans chaque branche, d'où $E_1 = \frac{Q_1}{C_1} = \frac{Q_2}{C_2}$ (0,5).

A.N. $Q_1 = 80 \mu\text{C}$ (0,25) $Q_2 = 240 \mu\text{C}$. (0,25)

2) $W_C = \frac{1}{2} \frac{Q_1^2}{C_1} + \frac{1}{2} \frac{Q_2^2}{C_2} = 12,8 \text{ mJ}$, (0,5)+(0,25)

3) $W_E = E_1(Q_1 + Q_2) = 25,6 \text{ mJ}$ (0,5)+(0,25), $W_J = W_E - W_C = 12,8 \text{ mJ}$. (0,5)+(0,25)

III) 1) $P = eI_0 + (R + r')I_0^2$ (01)

2) $157,5 = 20I_0 + 40I_0^2$, (0,25). Solution : $I_0 = 1,75 \text{ A}$ (01). et $I_0 = -2,25 \text{ A}$ (non physique) (0,25).

$E_2 = \frac{P}{I_0} = 90 \text{ V}$. (0,5)+(0,25)

Exercice 2

$$1) \vec{E}_M = K \frac{q_1}{(r+\frac{a}{2})^2} \vec{i} + K \frac{q_2}{(r-\frac{a}{2})^2} \vec{i} = K \left[\frac{q_1}{(r+\frac{a}{2})^2} + \frac{q_2}{(r-\frac{a}{2})^2} \right] \vec{i} \quad \boxed{(0,5)} \quad \vec{E}_M = K \frac{q}{a^2} \vec{i} \quad \boxed{(0,5)}$$

$$2) \text{ Conservation de l'énergie totale car la force électrique dérive d'un potentiel : } E_c(\frac{a}{2}) + E_p(\frac{a}{2}) = E_c(\frac{3a}{2}) + E_p(\frac{3a}{2}) \quad \boxed{(0,5)}$$

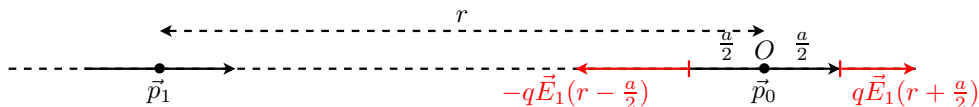
$$E_c(\frac{a}{2}) = 0 \text{ J} \quad \boxed{(0,25)}, \quad E_p(\frac{a}{2}) = K \frac{q_1 q_2}{a} = K \frac{3q^2}{4a} \quad \boxed{(0,5)},$$

$$E_p(\frac{3a}{2}) = K \frac{q_1 q_2}{2a} = K \frac{3q^2}{8a} \quad \boxed{(0,5)}, \quad \text{alors } E_c(\frac{3a}{2}) = K \frac{3q^2}{8a} \quad \boxed{(0,5)}$$

$$3) \text{ i) } \vec{E}_0 = 2K \frac{\vec{p}}{r^3} + 2K \frac{\vec{p}}{r^3} = 4K \frac{\vec{p}}{r^3} \quad \boxed{(0,5)}$$

$$\text{ii) } E_{p0} = -\vec{p} \cdot \vec{E}_0 = -4K \frac{p^2}{r^3} = -36 \cdot 10^{-21} \text{ J} \quad \boxed{(0,5)} + \boxed{(0,25)}$$

$$\text{iii) Champ créé par } \vec{p}_1 : \vec{E}_1(r) = 2K \frac{\vec{p}}{r^3}. \text{ Force } \vec{F} = -q\vec{E}_1(r - \frac{a}{2}) + q\vec{E}_1(r + \frac{a}{2}) \quad \boxed{(0,5)}$$



$$\vec{F} = -q2K \frac{\vec{p}}{(r-\frac{a}{2})^3} + q2K \frac{\vec{p}}{(r+\frac{a}{2})^3} = 2Kq\vec{p} \left[\frac{1}{(r+\frac{a}{2})^3} - \frac{1}{(r-\frac{a}{2})^3} \right] \quad \boxed{(0,5)}$$

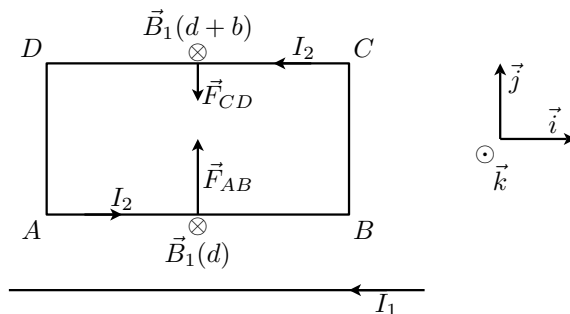
$$\text{(Notons que } \vec{F} \simeq -\frac{6Kq\vec{p}}{r^4}\text{)}$$

\vec{F} est dirigée vers \vec{p}_1 car $\left[\frac{1}{(r+\frac{a}{2})^3} - \frac{1}{(r-\frac{a}{2})^3} \right] < 0 \quad \boxed{(0,5)}$. De même la force exercée par \vec{p}_0 sur \vec{p}_1 est dirigée vers \vec{p}_0 (action-réaction) $\boxed{(0,5)}$. L'interaction est donc attractive. $\boxed{(0,5)}$

Exercice 3

$$1) \vec{F}_{AB} = \int_A^B I_2 d\vec{l} \wedge \vec{B}_1(y=d) \quad \boxed{(0,25)}. \text{ Donc } \vec{F}_{AB} = \frac{\mu_0 a I_1 I_2}{2\pi d} \vec{j}. \quad \boxed{(0,75)}$$

$$\vec{F}_{CD} = \int_C^D I_2 d\vec{l} \wedge \vec{B}_1(y=b+d) \quad \boxed{(0,25)}. \text{ Donc } \vec{F}_{CD} = -\frac{\mu_0 a I_1 I_2}{2\pi(b+d)} \vec{j}. \quad \boxed{(0,75)}$$



$$\vec{F} = \vec{F}_{AB} + \vec{F}_{CD} = \frac{\mu_0 I_1 I_2}{2\pi} \left[\frac{ab}{(b+d)d} \right] \vec{j} \quad \boxed{(0,25)}$$

$$2) \text{ Équilibre : } N \frac{\mu_0 I_1 I_2}{2\pi} \left[\frac{ab}{(b+d)d} \right] = mg \quad \boxed{(0,5)}. \text{ A.N. } m = \frac{\mu_0 N I_1 I_2}{2\pi g} \left[\frac{ab}{(b+d)d} \right] \simeq 1429 \text{ kg} \quad \boxed{(0,25)}$$